Greedy algorithms (contd.)

Average bit length  $(T) = \sum f_{x} \cdot depth_{x}(x)$ J RES prefixture S= Set of letters/Alphabet. We want to show that our algo goves an "optimal" prefix thee. Lemma: Our algorithm gives optimal prefix the. (Boot Knoof: By induction on IsI. Base case: Trivial case. 151= 1 Ind. hypothesis: 45, s.t. ISIEk-1, algo glives optimal prefix frees. Ind. step: Isl=k. 6 Algorithm generates a thee T. Suppose T is not optimal. JZ s.t ABL(Z) < ABL(T). -> Picks two least freq. letters y and z and replaced them w/ a letter w s.t for = fy+f2.  $S \longrightarrow S' s \cdot t | S' | = k - 1$ . ABL(T) =  $\sum f_2 \cdot depth_1(x)$ XES  $\uparrow \leftarrow \uparrow'$ = Z f\_2. depth(a) 2ES\{y,z{ + fy. depth(y) + fz. depth(z)





Strategy: Pick veg w/ early findsh tomes. Algo: Input: R, a set of requests  $A \leftarrow \phi$ . While R is not empty: Choose a veg i w/ lowest findsh tome. A - AU{iz. Remove all reas incompatible w/i in R, along w/i. Smaxinisze The no of jobs/vegs that are compatible w/ each other. Ketwan A. Correctness: A le optimal. Say there exists a subset OER sit O is optimal.  $O = \{J_{n}, \dots, J_{m}\}$   $A = \{I_{n}, \dots, I_{k}\}$   $(\omega) - f(\omega)$ , in sorted order of their tomes. If O is optimal, m>k. IF A is not optimal, m>k. We want to asgne that in connot be staticity larger than k if A was built whing our algorithm.  $O = \{J_1, \ldots, J_k\}, \ldots, J_m\}$ Obs:  $f(I_{i}) \leq f(J_{i})$ .  $A = \{I_1, \dots, (I_k)\}$ Lemma:  $\forall r \leq k$ ,  $f(I_r) \leq f(J_r)$ . > JRH .... Jun ave compatible w/ A.

